

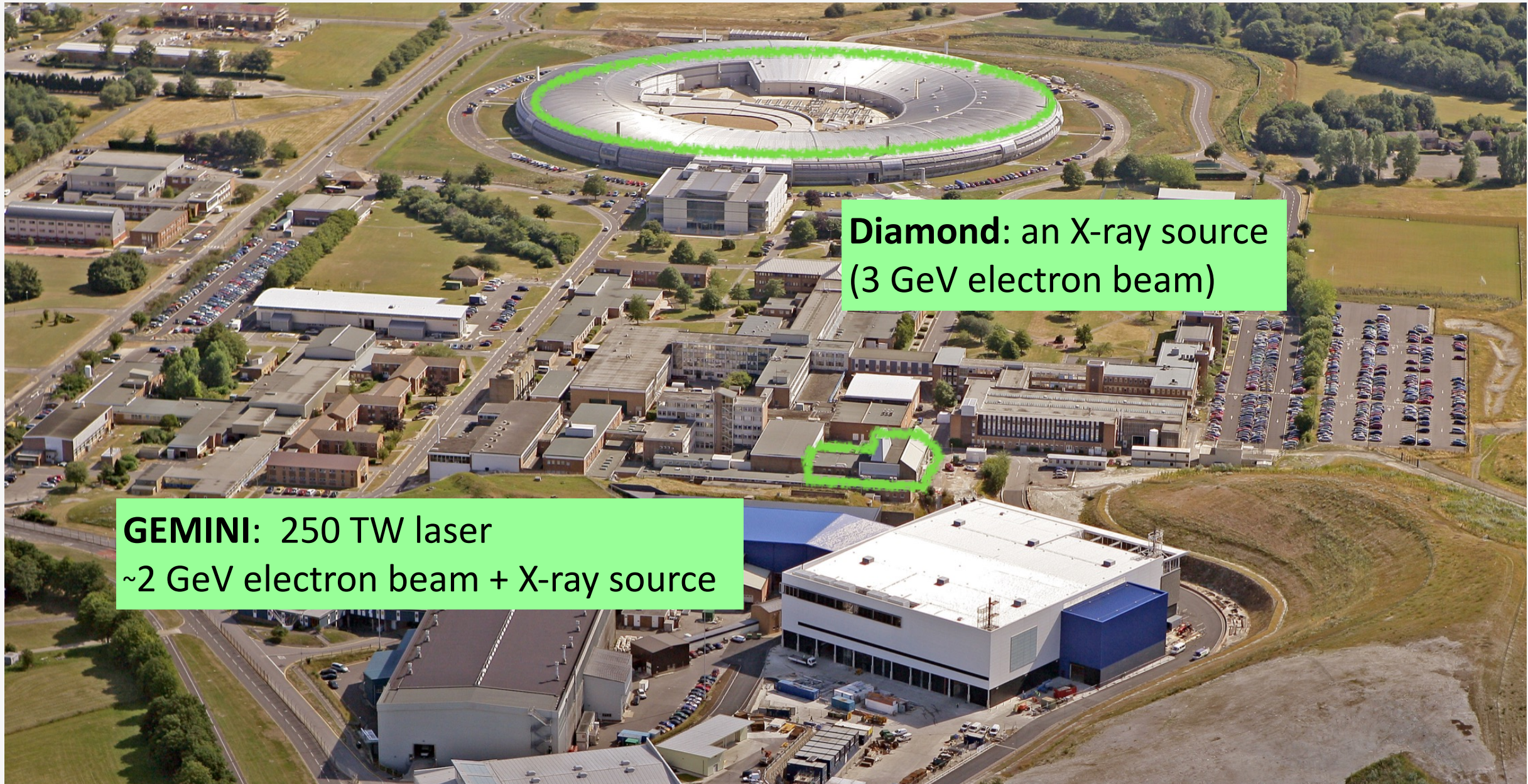
**IMPERIAL**

# Laser Wakefield Accelerators: Tools for Time-Resolved X-Ray Imaging and Spectroscopy

Stuart Mangles  
23/04/2024

# Outline

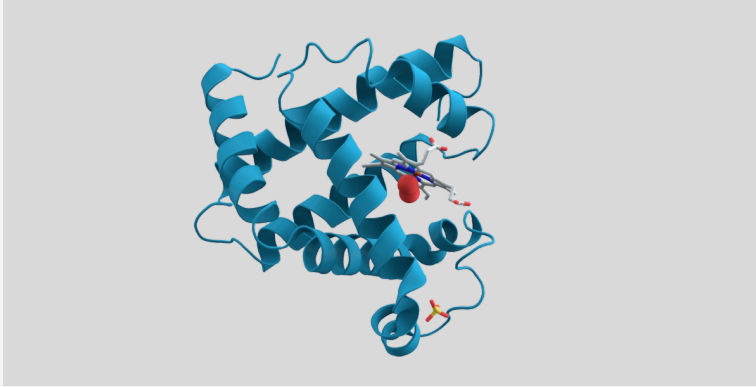
- 1 Intro to laser wakefield accelerators
- 2 Basic concepts of X-ray generation
- 3 Synchrotron radiation from Laser Wakefield Accelerators
- 4 Applications of X-rays from Laser Wakefield Accelerators



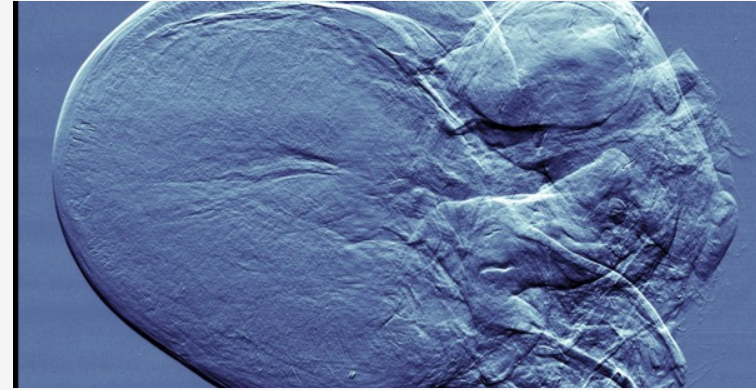
**Diamond: an X-ray source  
(3 GeV electron beam)**

**GEMINI: 250 TW laser  
~2 GeV electron beam + X-ray source**

# X-rays are amazing tools for science



Myoglobin structure calculated using x-ray crystallography, wikipedia.org

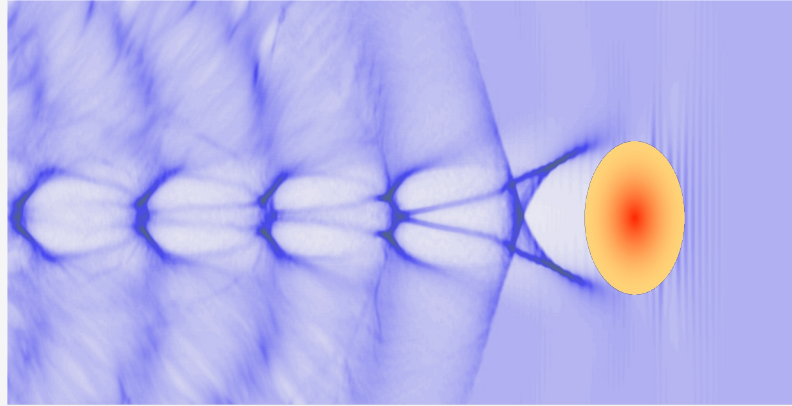


High resolution phase contrast x-ray imaging of a rat's heart  
F. Pfeiffer. C. David, www.cimst.ethz.ch

## **Bright x-rays produced by particle accelerators are used a tool by a huge variety of scientists**

- X-ray diffraction used to work out structures of proteins vital for discovery of new drugs, magnetic materials ...
- Advanced x-ray imaging techniques to improve medical diagnosis
- X-ray tools used in palaeontology and archaeology

# Laser wakefield accelerators



10-30  $\mu\text{m}$  Laser pulse 



## Laser wakefields are compact laser-plasma accelerators

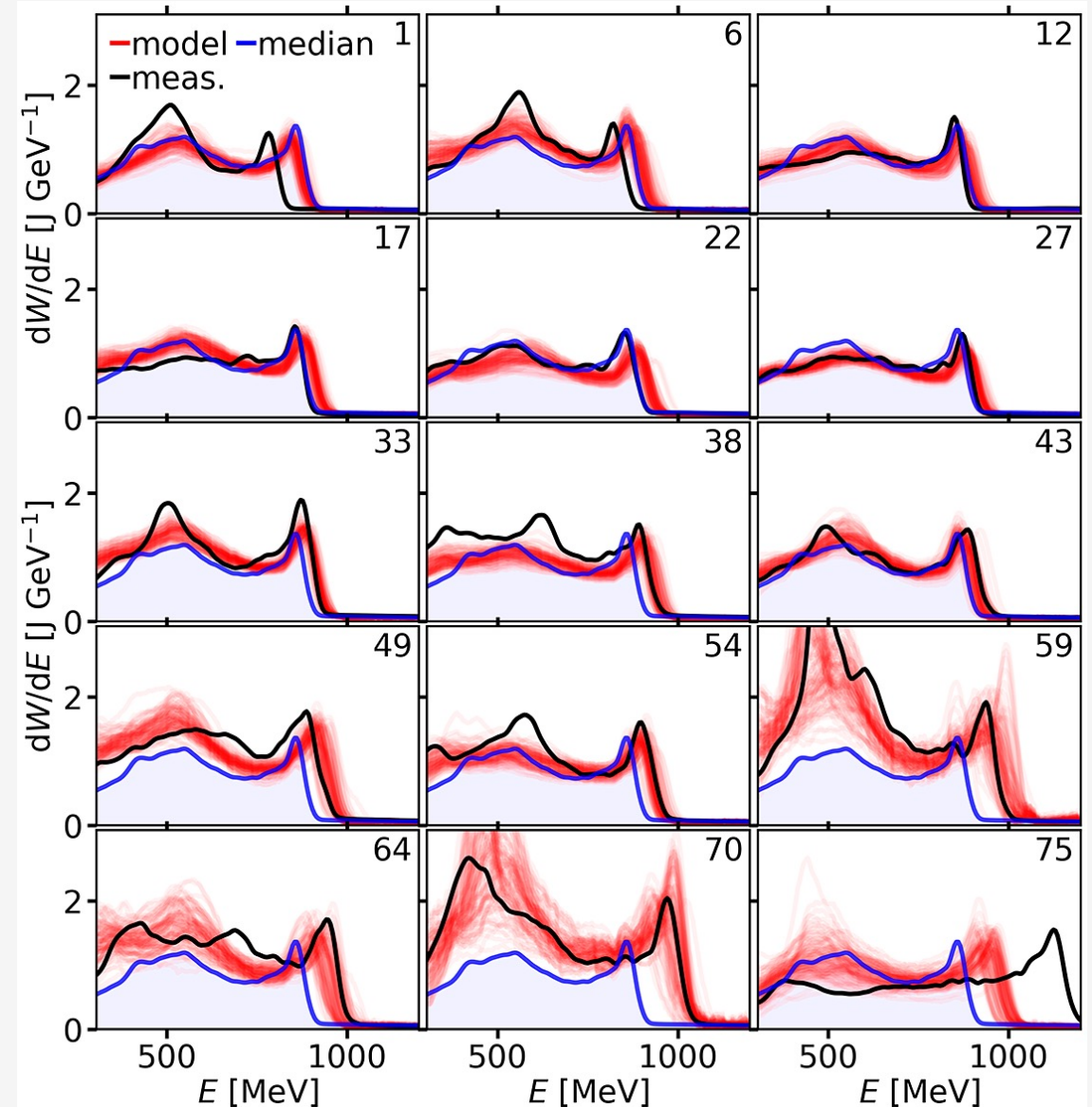
- Plasma wave driven by very intense laser pulse travelling through a plasma
  - Plasma waves can support fields  $> 100 \text{ GV m}^{-1}$
  - conventional accelerators are limited to  $< 100 \text{ MV m}^{-1}$

# Laser wakefield accelerators

## What sort of electron beams can we get?

Electron beam properties:

- giga-electronvolt energy
- femtosecond duration
- Image shows selection of electron spectra from Gemini
  - Black: measured spectrum
  - Red: predictions of spectrum predicted by neural net based on other diagnostics of laser + plasma
  - Blue: average spectrum



# Basic Concepts of X-ray Generation

# X-ray Generation Mechanisms

There are many mechanisms for X-ray generation

- Bremsstrahlung
- Characteristic radiation (K-alpha etc)
- Synchrotron Radiation
- Thomson scattering
- Free Electron Lasers

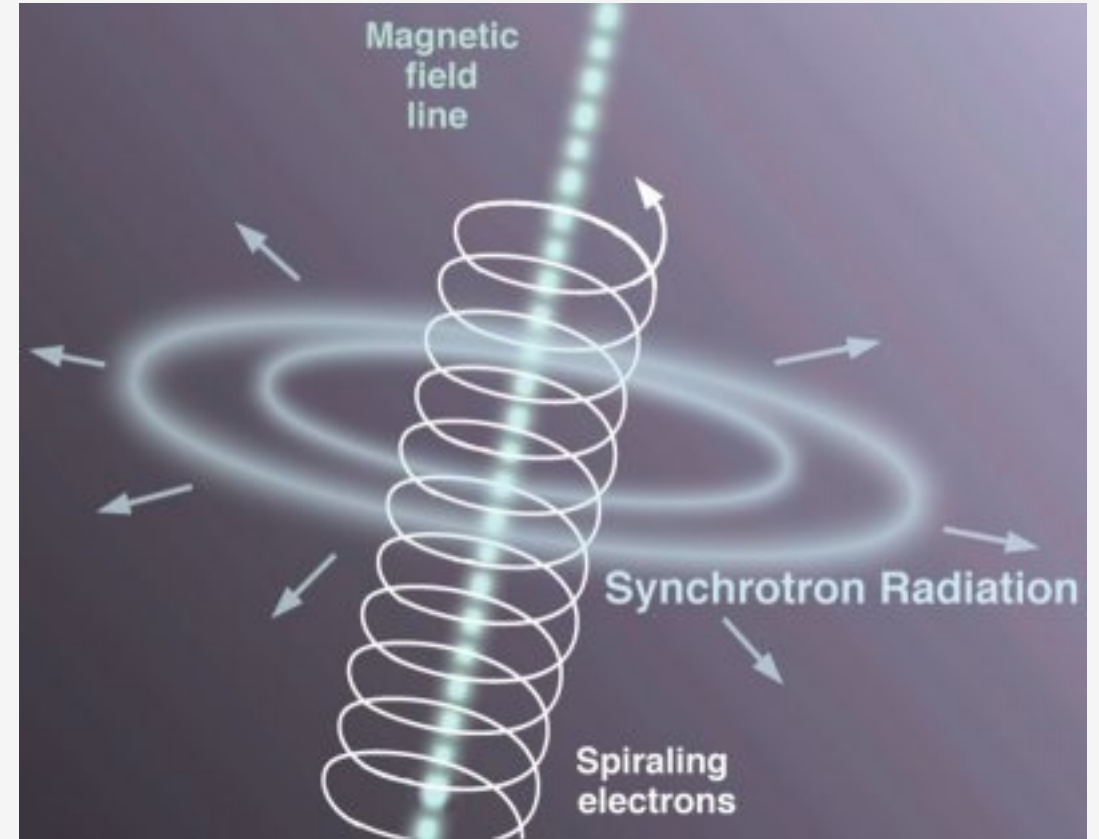


Image: Jon Lomberg/Gemini Observatory.



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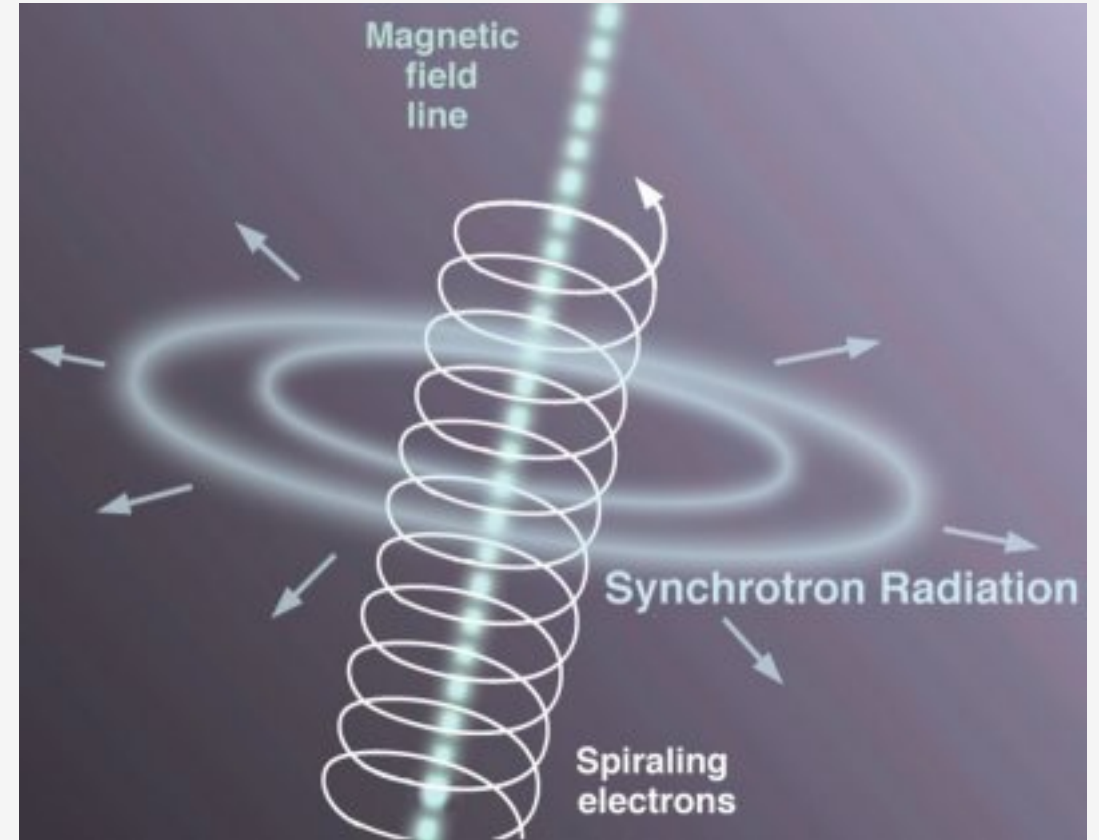


Image: Jon Lomberg/Gemini Observatory.

# X-ray generation with high-energy electron beams

## For high-energy electron beams ( $E \gg m_e c^2$ )

- Radiated power given by relativistic Larmor formula
- High energy particles radiate **a lot**
- High energy particles have  $|\underline{\beta}| \rightarrow 1$ :  
radiation is generated by bending the beam
- For constant circular motion (radius R) the expression is simpler

$$P = \frac{q^2}{6\pi\epsilon_0 m^2 c^3} \gamma^6 \left[ (\dot{\underline{\beta}})^2 - (\underline{\beta} \times \dot{\underline{\beta}})^2 \right]$$

$$P = \frac{e^2 c}{6\pi\epsilon_0} \frac{\beta^4 \gamma^4}{R^2}$$

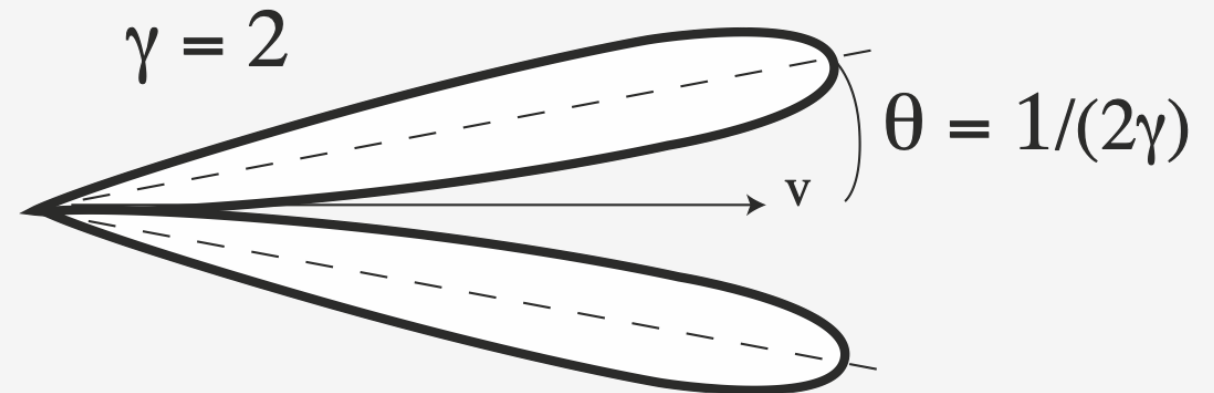
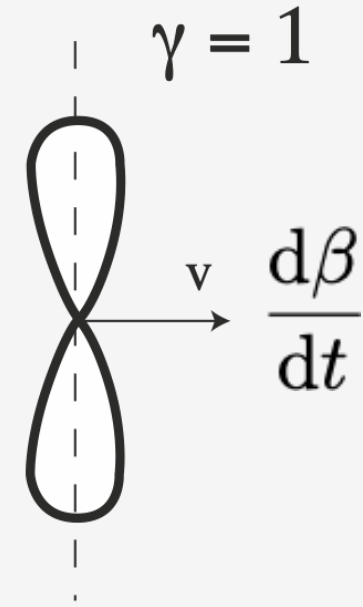
Power radiated by moving charge (Jackson chapter 14)

# X-ray generation with high-energy electron beams

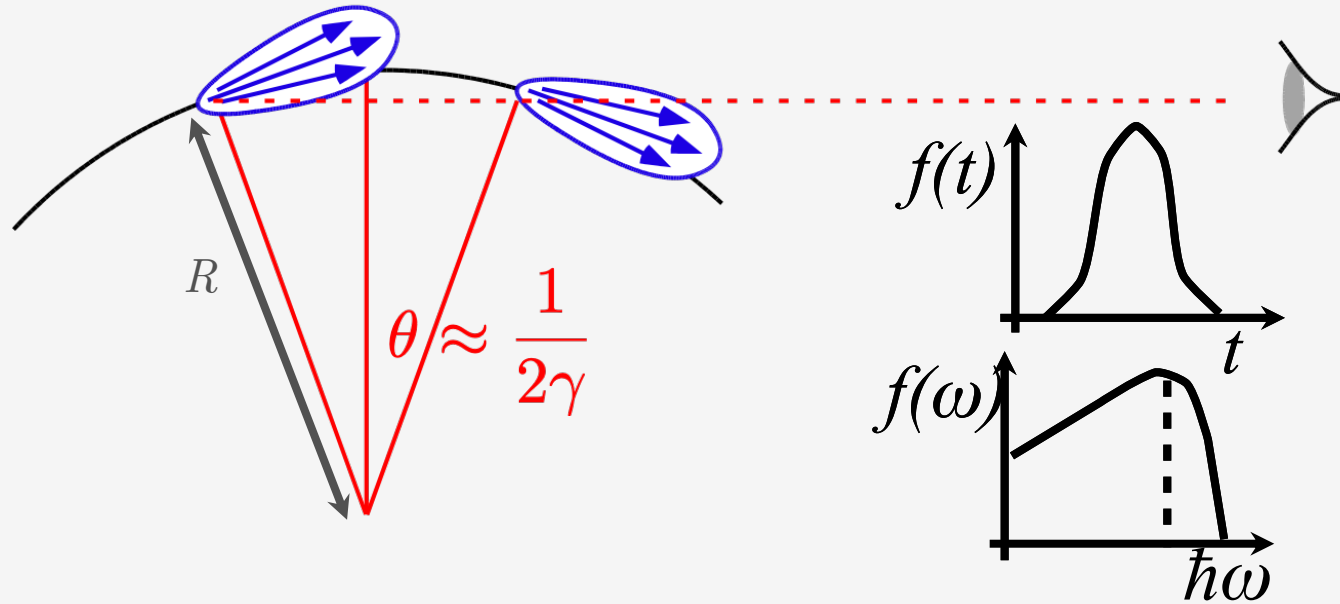
Radiation from **low-energy** electrons is emitted perpendicular to beam direction

Radiation from **high-energy** electrons is “beamed” into narrow cone

- beam of X-rays pointing along the electron beam trajectory



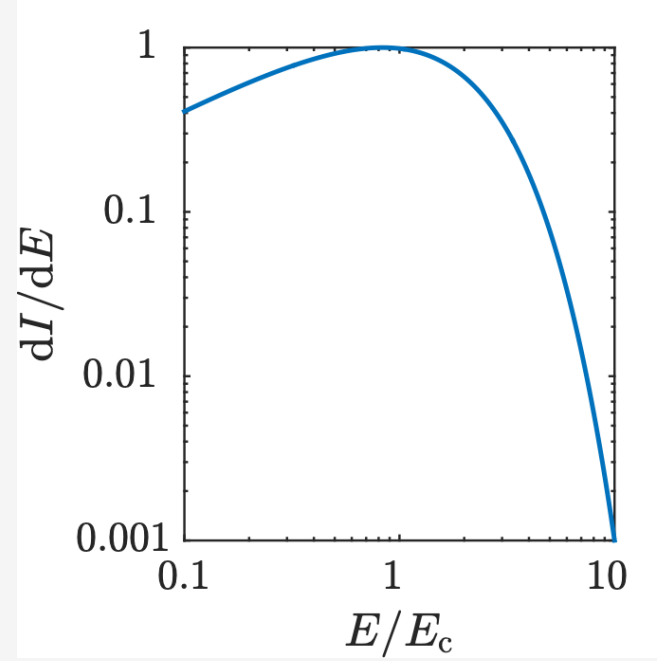
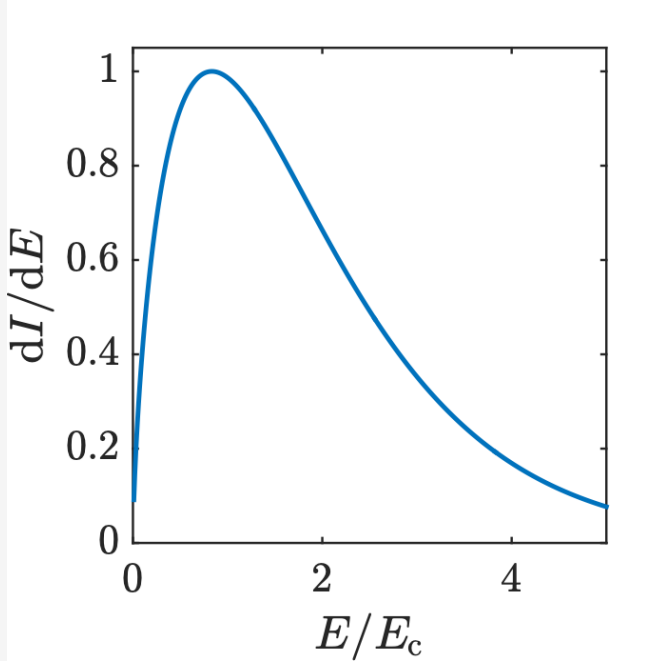
# Radiation from particle in circular motion



- Observer sees radiation flick on and off as beam sweeps past
- Duration of “flash” determined by radius of circle,  $R$  and the electron Lorentz factor,  $\gamma$
- Spectral bandwidth of the radiation found from time bandwidth product
  - This determines the critical photon energy,  $E$

**for high-energy X-rays we need high  $\gamma$  and small  $R$**

# Synchrotron Radiation Spectrum



Critical energy,  $E_c$  is a single parameter that defines shape of Synchrotron radiation

Radiation “on-axis”

$$\frac{d^2 I}{dE d\Omega} = \frac{3e^2}{16\pi^3 \epsilon_0 c} \gamma^2 \left( \frac{E}{E_c} \right)^2 K_{2/3}^2 \left( \frac{E}{2E_c} \right)$$

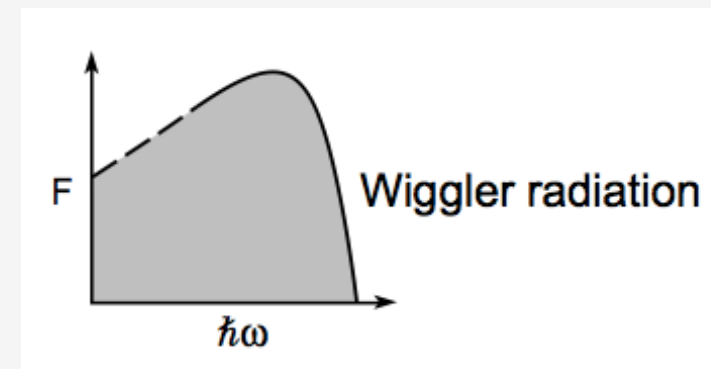
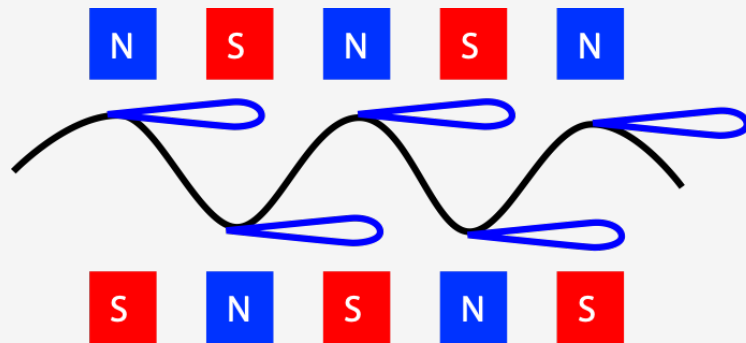
$$E_c = \frac{3}{2} \hbar c \gamma^3 / R$$

# Wigglers and Undulators radiation

To get more X-rays add more bends

Define K parameter:  $K = \gamma k_0 r_0$

**Wiggler:** if  $K \gg 1$ : spectrum is still synchrotron-like

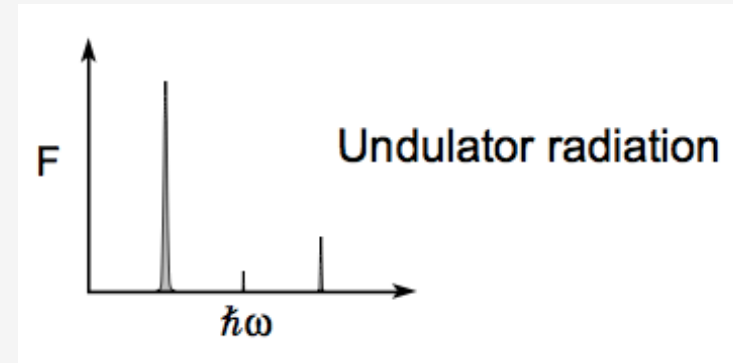
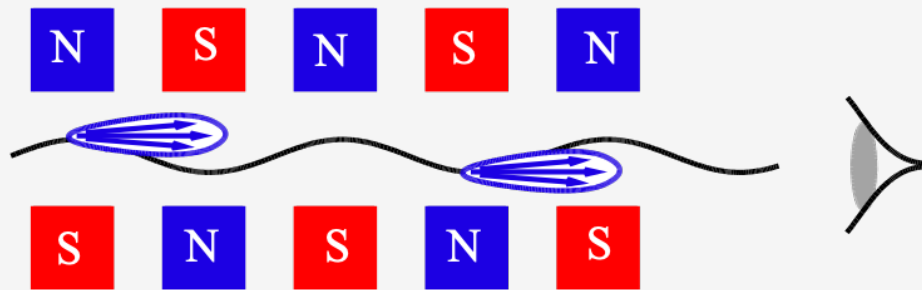


# Wigglers and Undulators radiation

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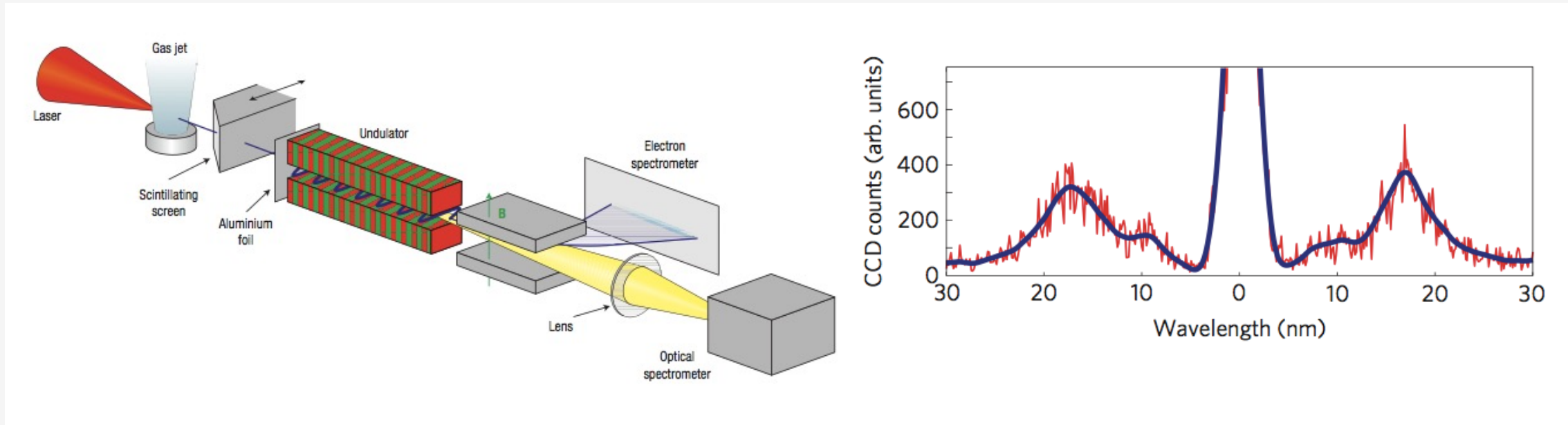
**Undulator:** if  $K \ll 1$ : spectrum is monochromatic



# Synchrotron radiation from laser wakefield accelerators



# Radiation using conventional undulator



Fuchs Nature Phys 2009  
Schlenvoigt Nature Phys 2008

LWFA producing  $\approx 200$  MeV beams used in conventional undulator

- few centimetre period
- soft X-rays ( $< 100$  eV)

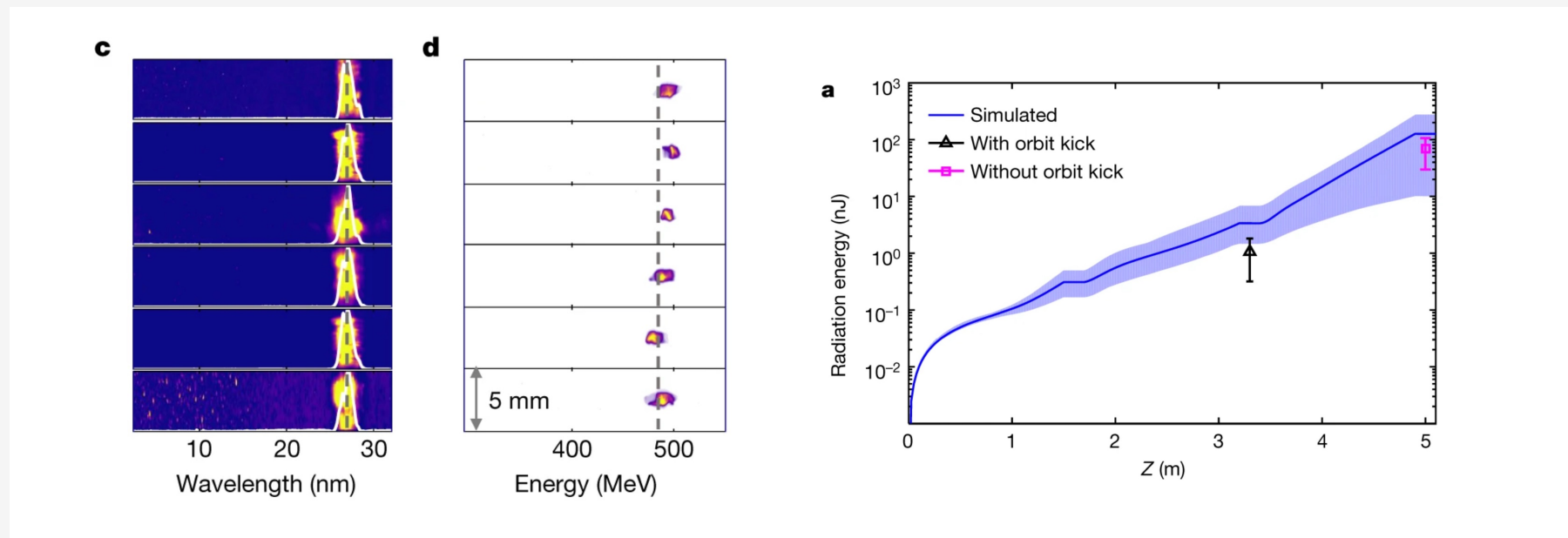
**Need shorter period to reach keV X-rays  
But these are the route to LWFA FELs**

# 2021/22 was the year of the plasma FEL

2.7 nm FEL at SIOM: Wang et al Nature **595**, 516 (2021)

0.8  $\mu\text{m}$  FEL at Frascati: Pompili et al Nature **606**, 659 (2022)

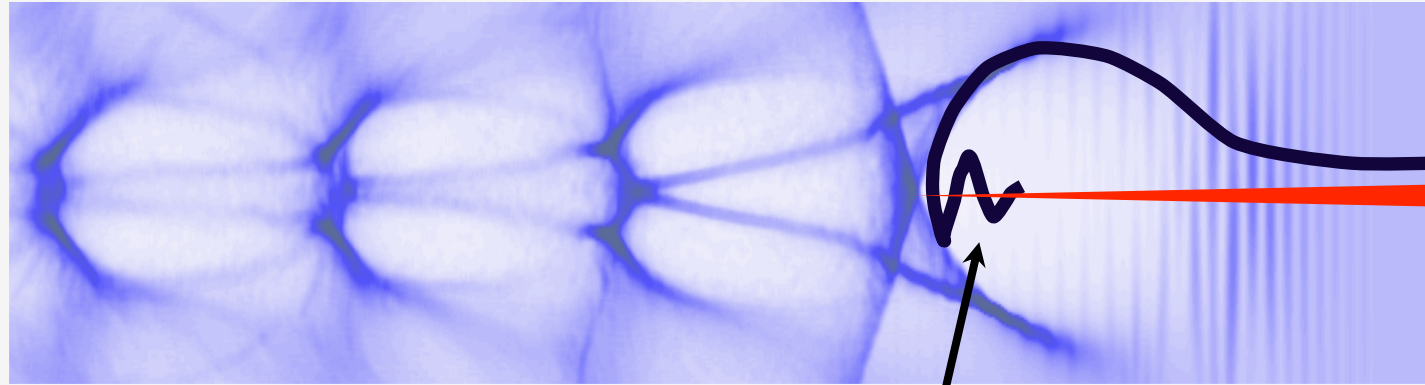
270 nm seeded FEL at HZDR: Labat et al Nature Photonics (2022)



**But can we use LWFA to reach keV X-rays?**

# Laser Wakefield as accelerator and wiggler

electron density of high amplitude plasma wave



trapped electron trajectory

bright X-ray flash

betatron oscillations

Strong transverse fields inside bubble make electrons oscillate while being accelerated

- “betatron oscillations”

- wavelength of oscillations can be very short compared to conventional wigglers

- for  $n_e = 10^{19} \text{ cm}^{-3}$  and 200 MeV electrons this is 300  $\mu\text{m}$

$$\omega_\beta = \frac{\omega_p}{\sqrt{2\gamma}} \quad \lambda_\beta = \sqrt{2\gamma} c / \omega_p$$

# Energy of X-rays from a Laser Wakefield Accelerator

Energy of X-rays in synchrotron:

$$E_c = \frac{3}{2} \hbar c \gamma^3 / R$$

We can rewrite R in terms of the wiggler wavelength and amplitude

$$R \approx 1 / (k_\beta^2 r_\beta) \quad \omega_\beta = \frac{\omega_p}{\sqrt{2\gamma}}$$

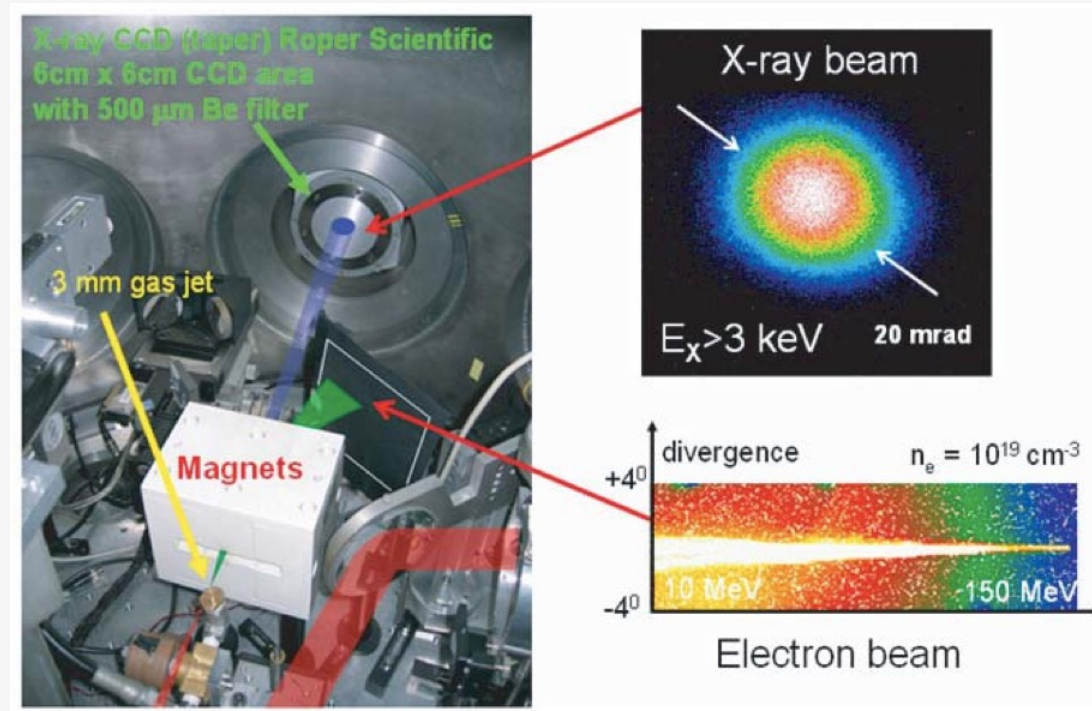
Result is expression for critical energy for x-rays from a LWFA:

$$E_c = \frac{3}{4} \hbar \gamma^2 \omega_p^2 r_\beta / c$$

Typical values for a laser wakefield accelerator:

- $r_\beta \simeq 1 \mu\text{m}$ ,  $\gamma \simeq 2000$ ,  $n_e \simeq 10^{18} \text{ cm}^{-3} \rightarrow E_c \simeq 10\text{s keV}$

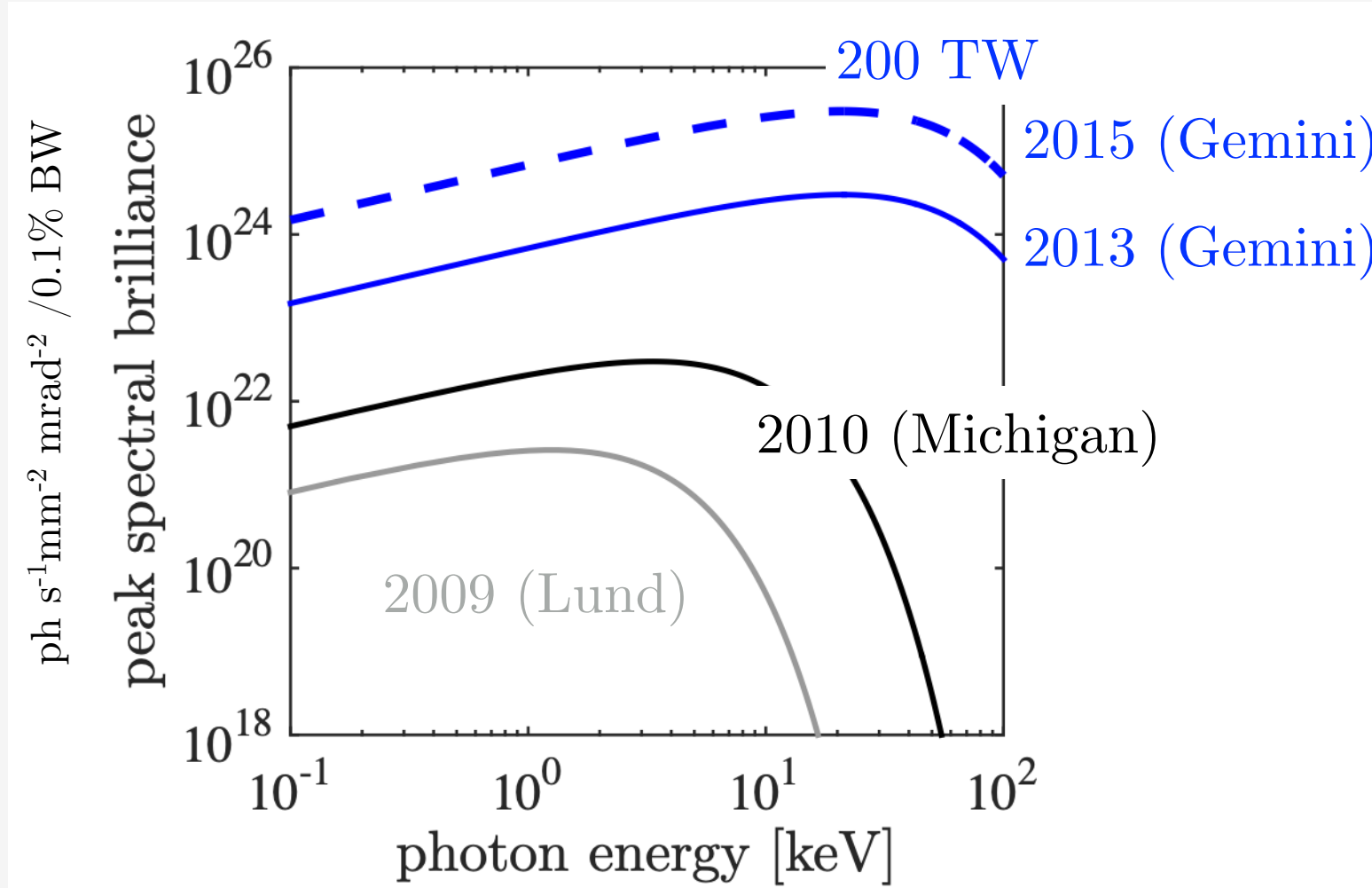
# X-rays from a laser wakefield accelerator



## First observed by Rouse *et al.* at LOA (PRL 2004)

- 30 TW laser
- broad band  $\simeq 100 \text{ MeV}$  electrons
- X-ray radiation at  $\simeq 1 \text{ keV}$

# X-ray energy and brightness scale with electron beam energy



Experiments have rapidly increased X-ray flux and photon energy

# Applications of X-rays from Laser Wakefield Accelerators

# What properties do X-rays from LWFA have that we can exploit?

## **Co-location of electron / X-ray source with other high-power lasers**

- ns pulses for shock compression
- fs and ps pulses to produce hot / warm dense matter

## **Natural synchronization of electron / X-ray source with these lasers**

- fs synchronization routinely achieved

## **Unique properties of LWFA source**

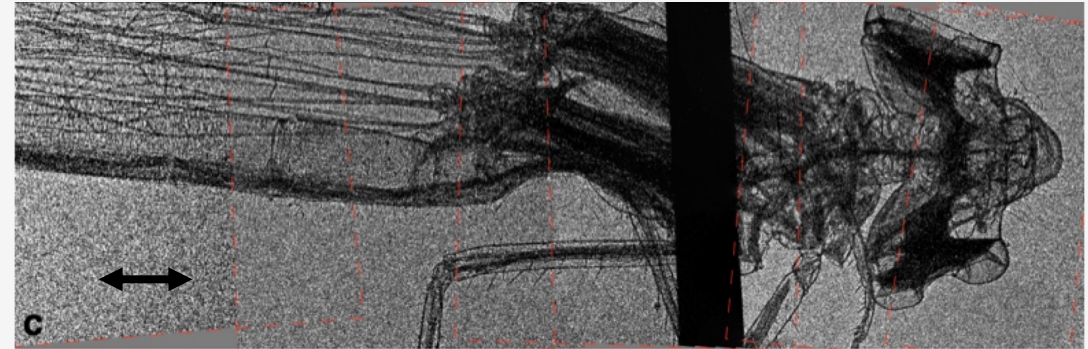
- X-ray source is small ( $\approx 1 \mu\text{m}$ )
- X-rays are both broadband and ultra-fast ( $\approx 10\text{s fs}$ )



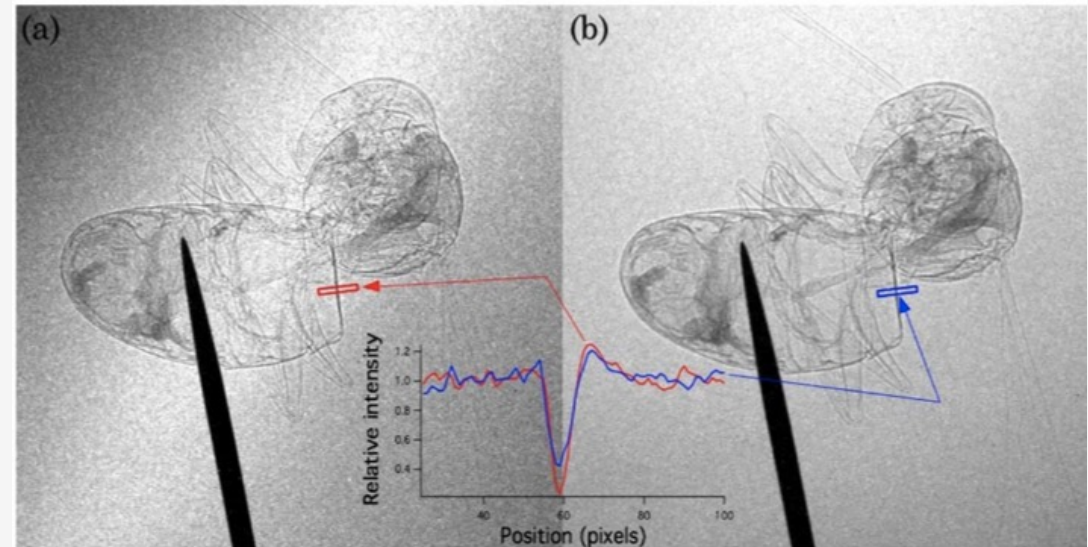
# Small Source size good for imaging

high definition, high resolution imaging using phase contrast or absorption contrast

- possible because of the very small source size
- images possible in a single shot (30 fs exposure)

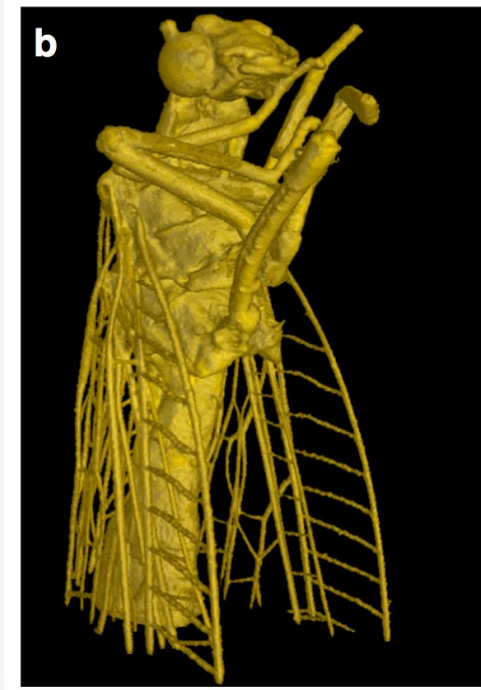


Kneip Applied Physics Letters 2011



Fourmaux Optics Letters 2011

# X-rays now stable enough to perform 3D tomography



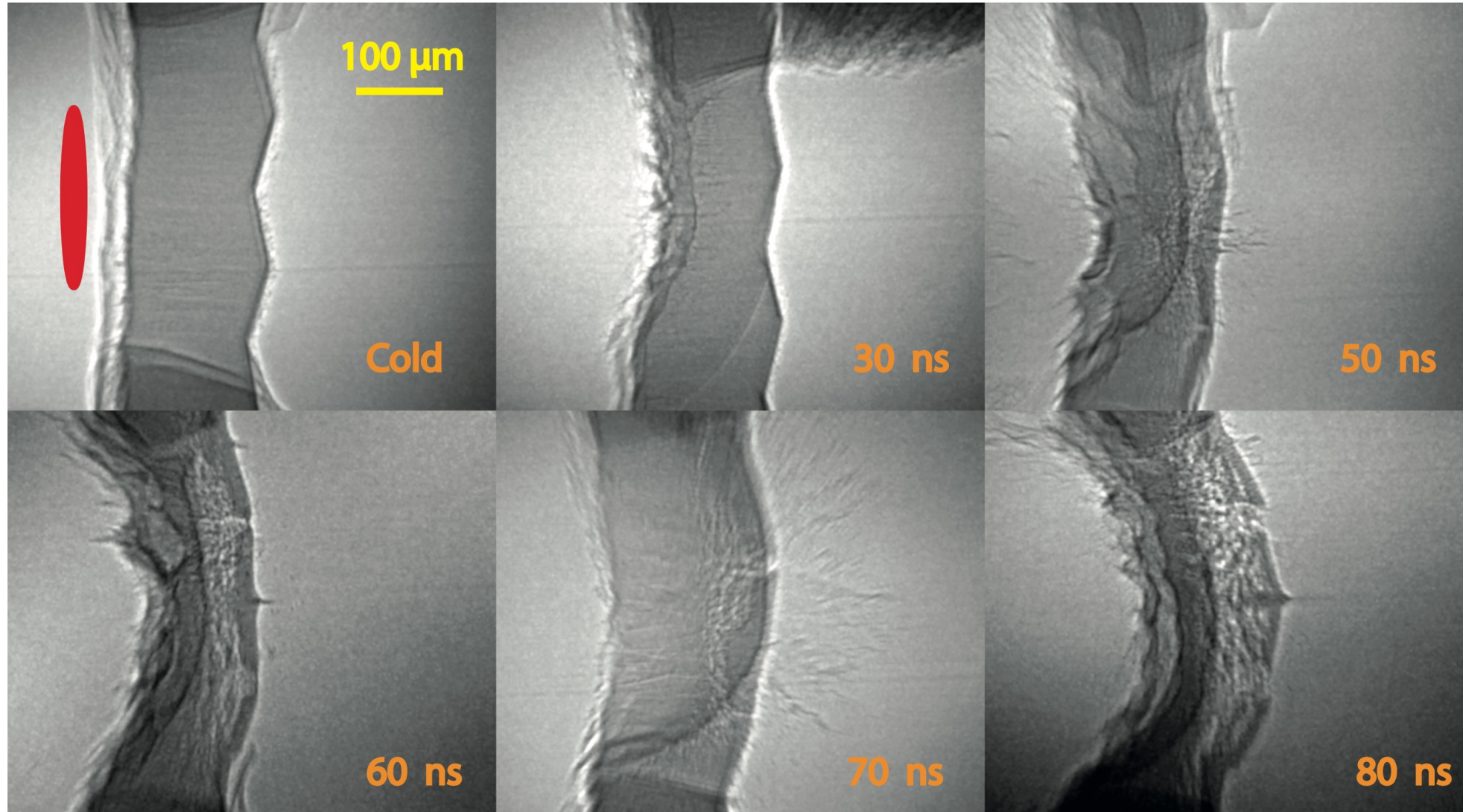
Wenz et al, Nature Comms 2015



Cole et al, Sci. Rep. 2015

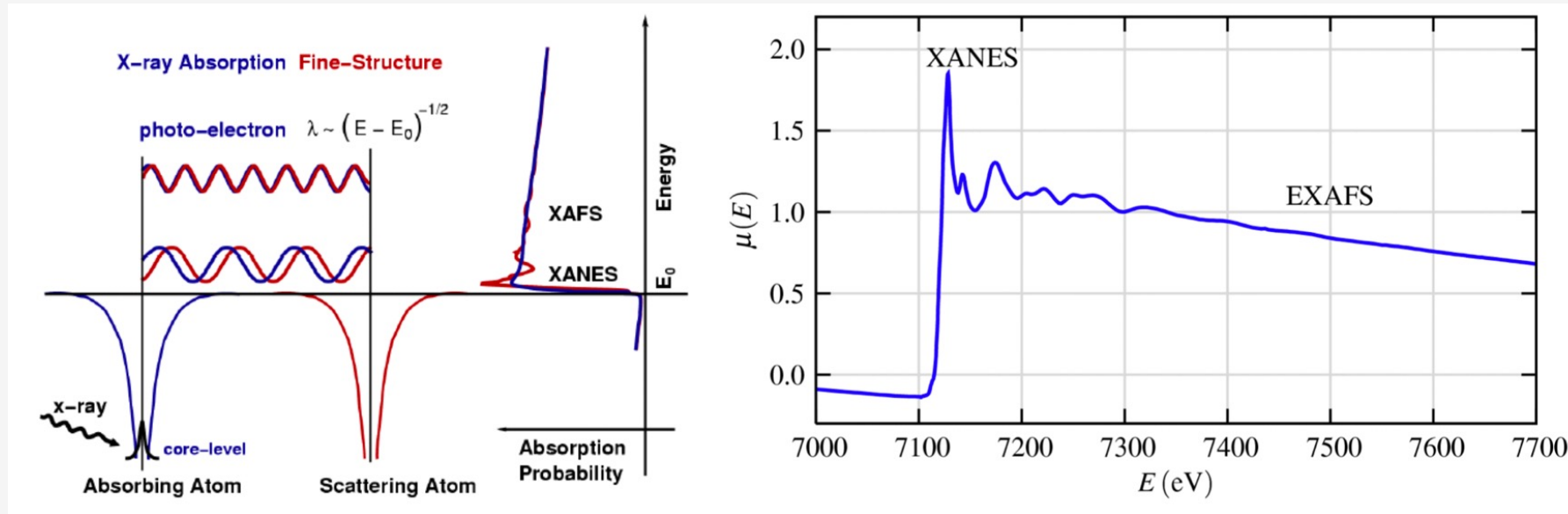
- Tomography requires acquisition of 100s images per sample
- LWFA sources already competitive with state of the  $\mu$ CT
- High rep rate LWFA an exciting prospect for rapid tomography scans

# Imaging rapidly evolving phenomena: laser driven shocks on Gemini



See J Wood Sci Rep 2018

# An ultrafast XANES / EXAFS diagnostic based on LWFA?



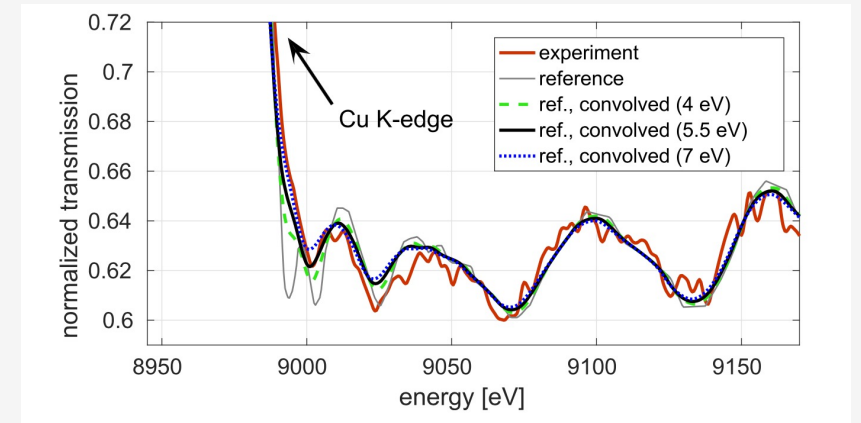
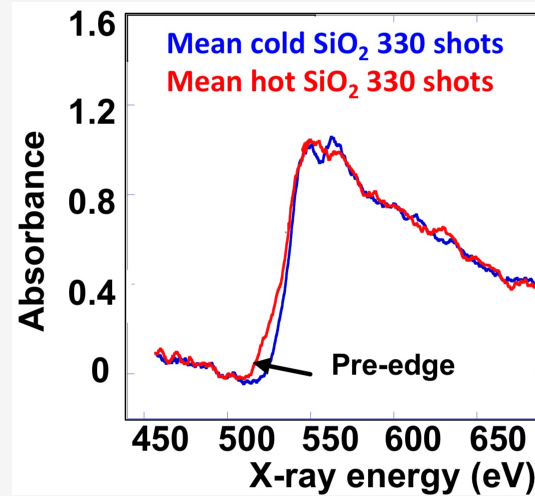
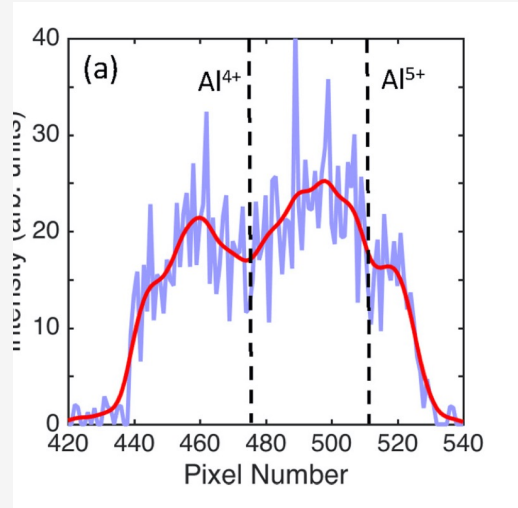
A Practical Introduction to Multiple Scattering Theory, Bruce Ravel, 2005

X-ray Absorption Spectroscopy is a powerful technique that provides a wealth of data about the properties of condensed matter

- X-ray is absorbed, produces photo-electron
- If Debroglie wavelength of photo-electron larger than spacing between absorbing atom and nearest neighbours, interference leads to peaks and troughs in absorption

**Unique combination of broad spectrum and fs duration makes LWFAs ideal**

# X-ray absorption spectroscopy using LWFA



## Mo PRE 2017

- 80 TW laser pulse
- 150 shots per spectrum

## Albert IPAC 2018

- 20 TW laser pulse
- 300 shots per spectrum

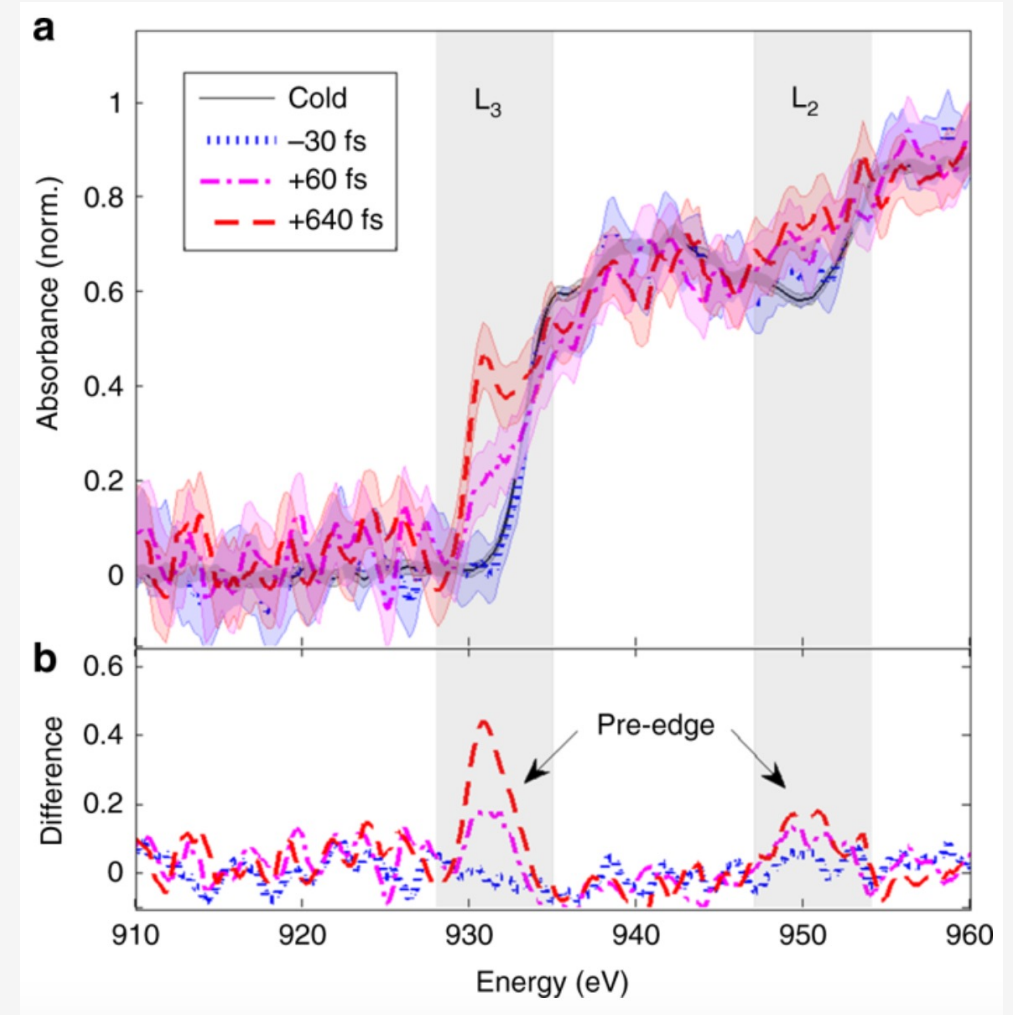
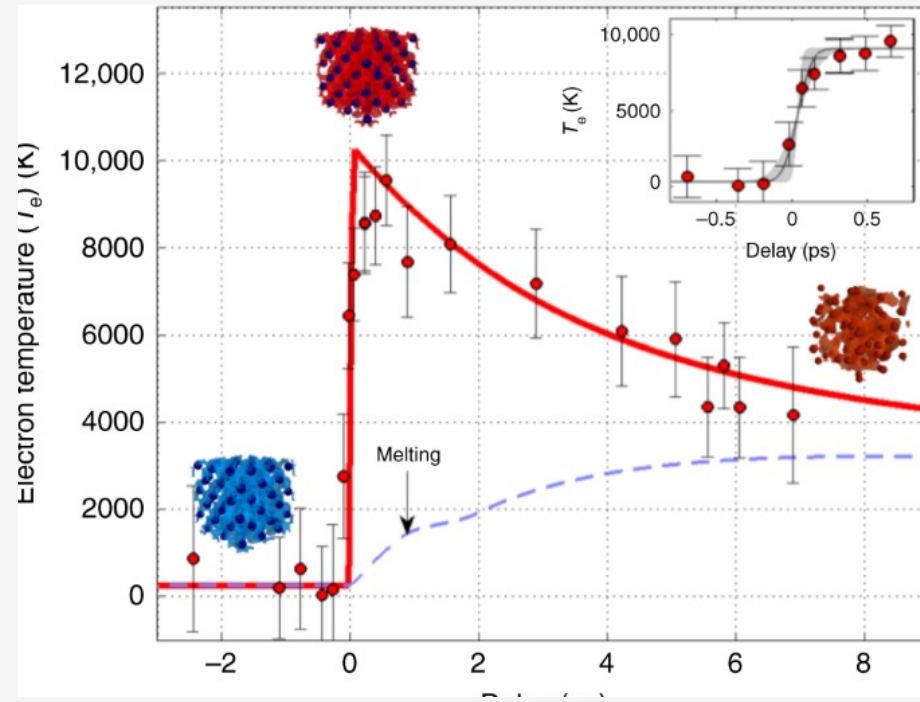
## Smid Rev Sci Inst 2017

- 20 TW laser
- 150 shots per spectrum

# X-ray absorption spectroscopy using LWFA

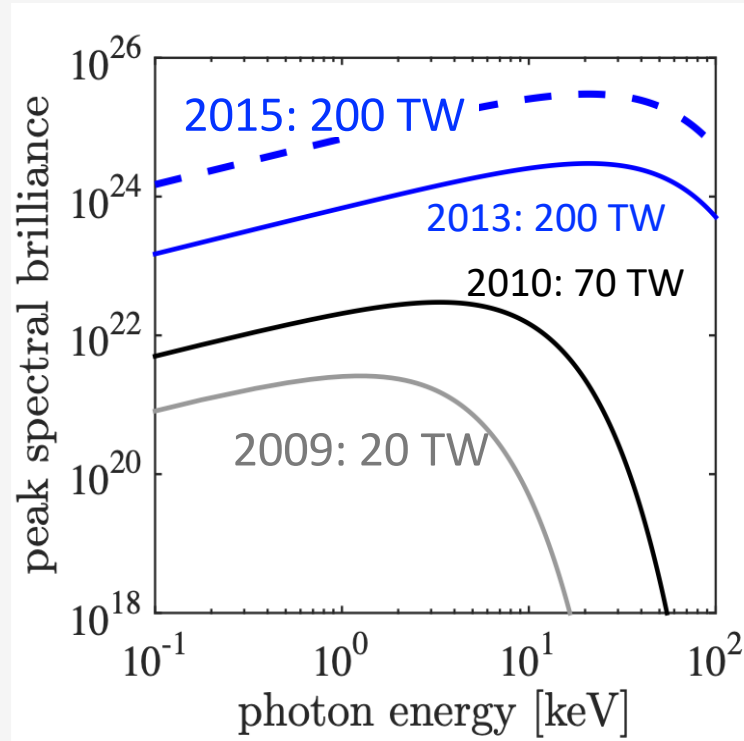
## Mahieu Nat Comms 2018

- 50 TW laser
- 50 shots per spectrum



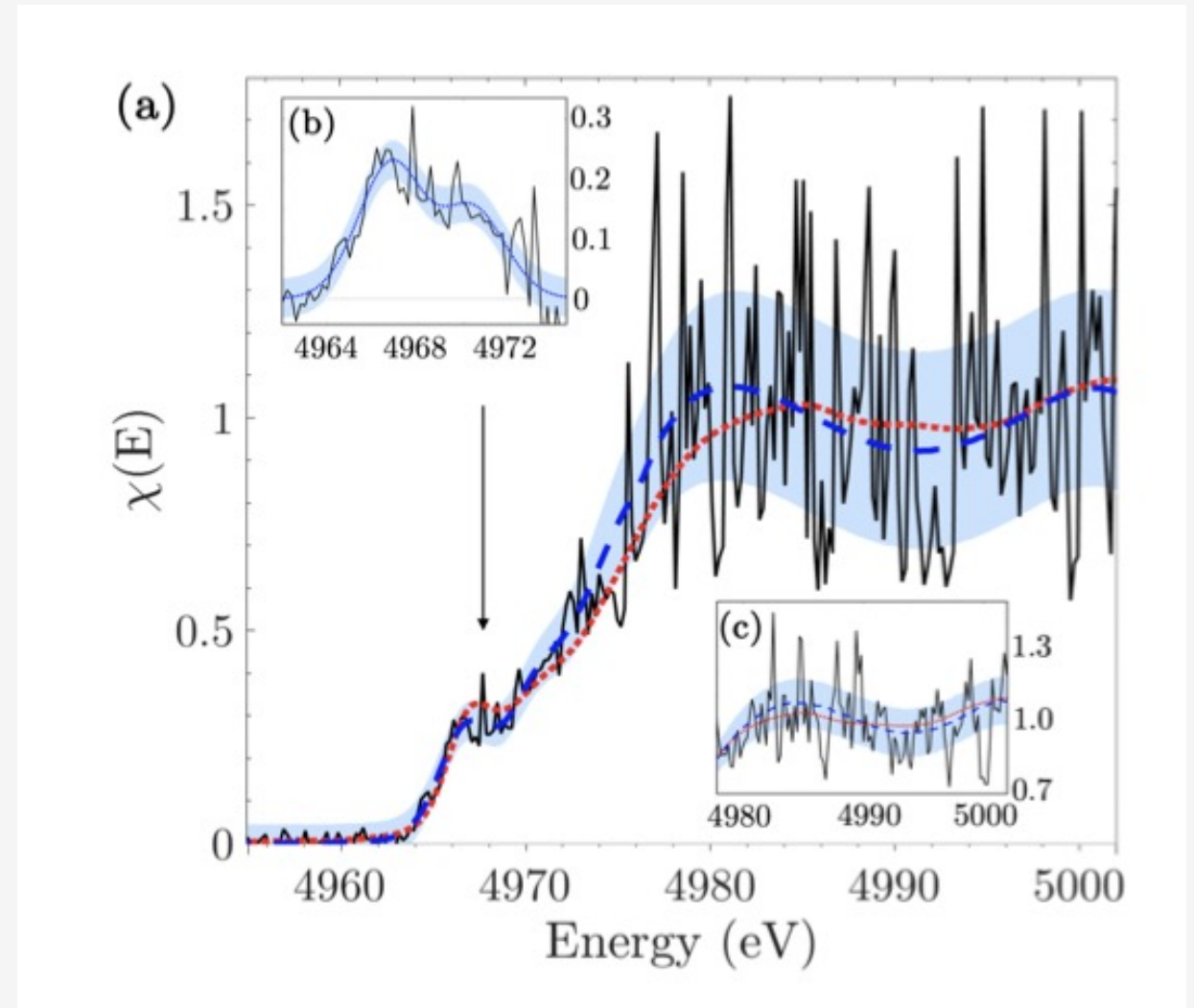
# Single shot X-ray absorption spectroscopy

## Single shot XANES

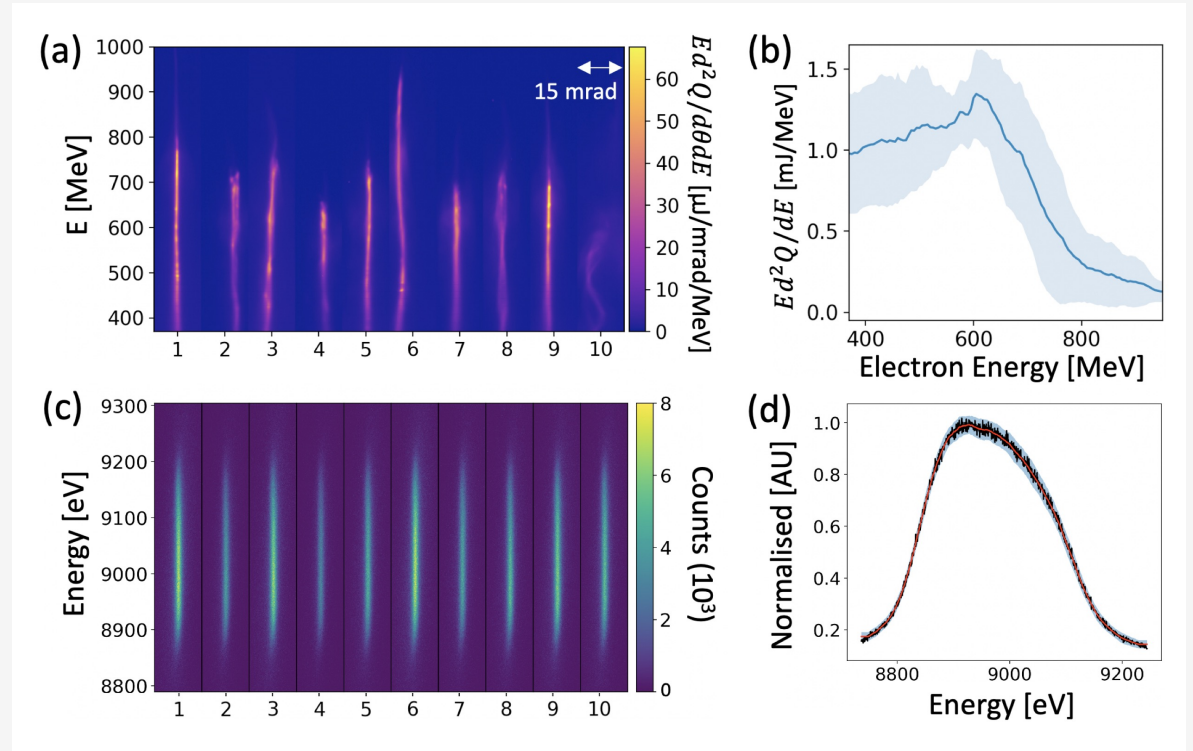
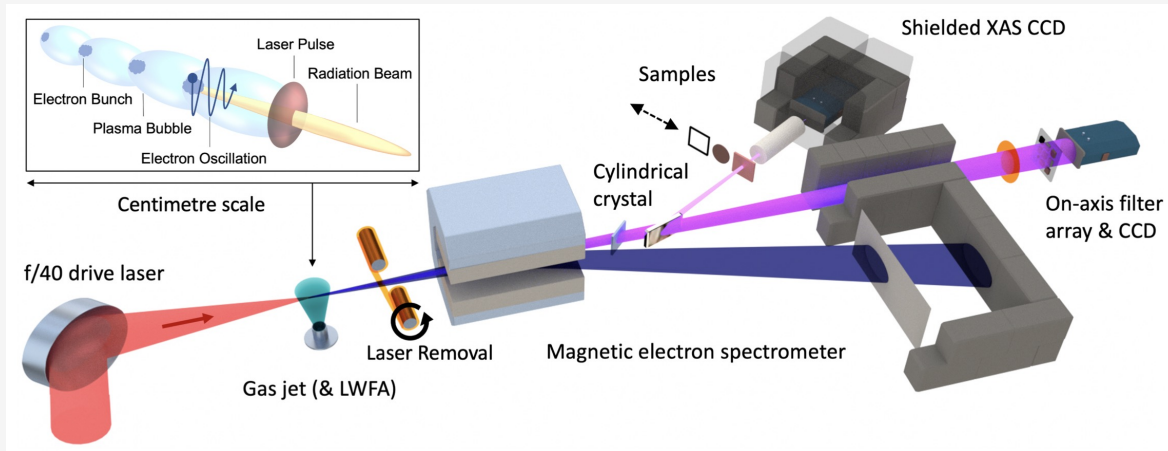


### Kettle PRL 2019

- 250 TW laser pulse
- Single shot XANES



# Single shot X-ray absorption spectroscopy



## Kettle 2023 arXiv:2305.10123

- New geometry to improve signal:noise
- Stable x-rays (despite electron beam fluctuations)

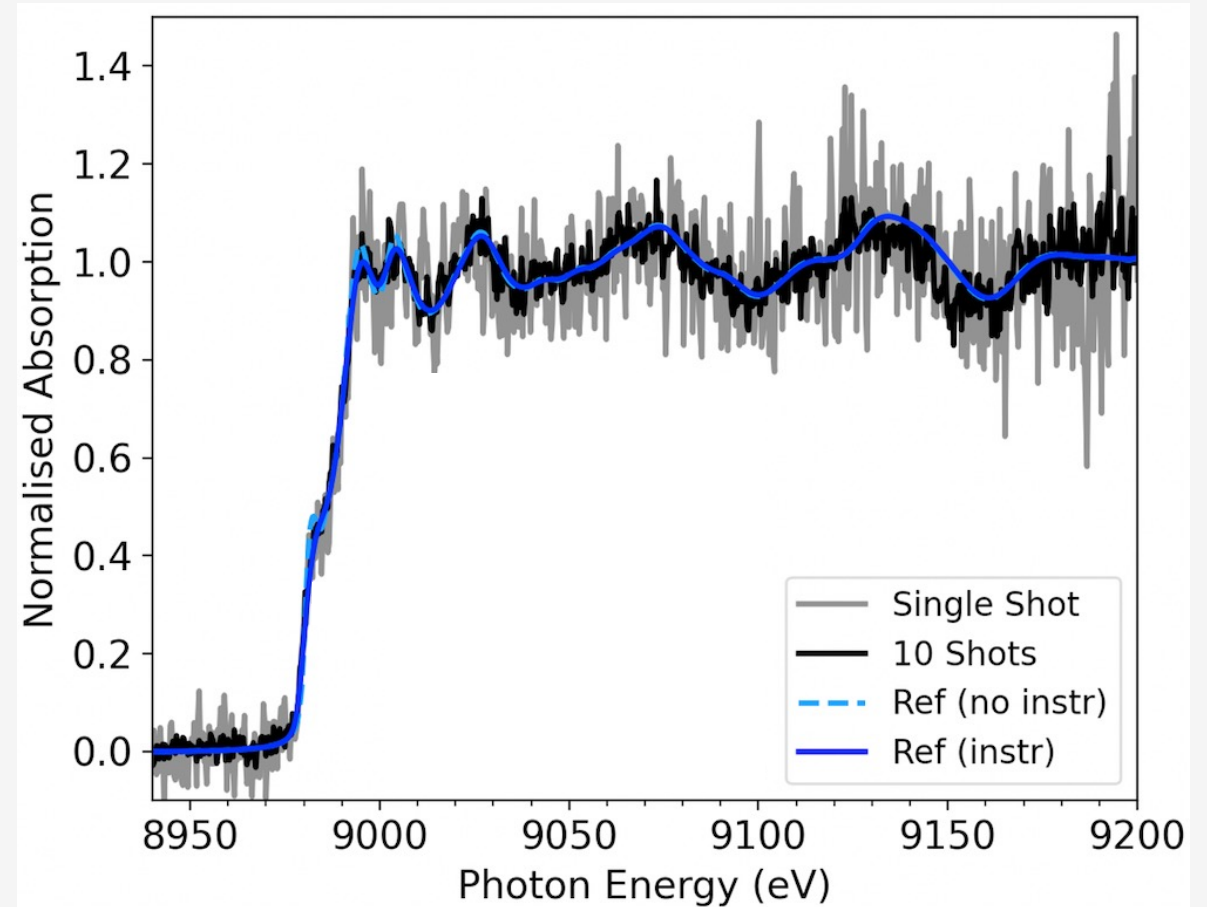


# Single shot X-ray absorption spectroscopy

## Single shot EXAFS and XANES

### Kettle 2023 arXiv:2305.10123

- 250 TW laser pulse
- Single shot XANES *and* EXAFS

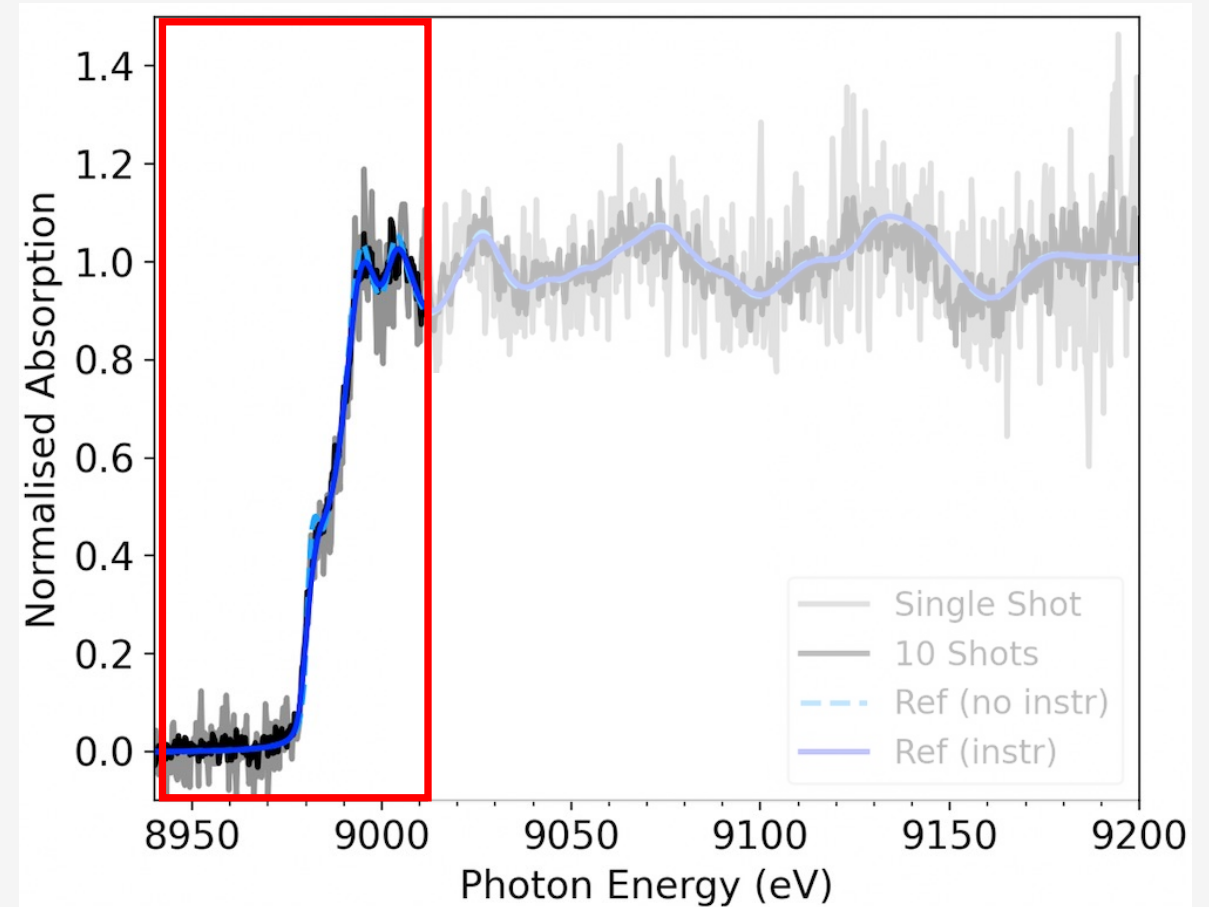


# Single shot X-ray absorption spectroscopy

## Single shot EXAFS and XANES

### Near edge

- information about the electrons (XANES)
  - electron distribution function, density of states, electron temperature

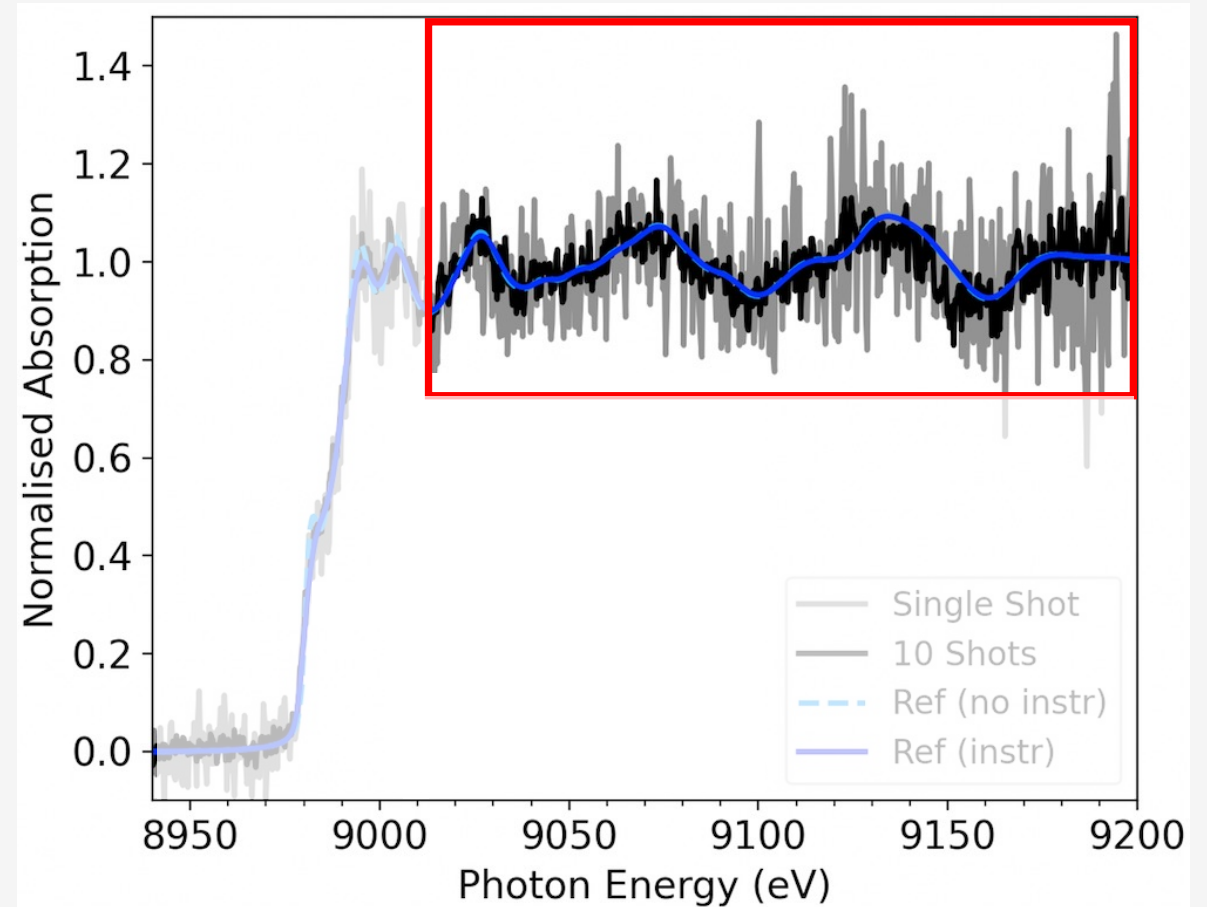


# Single shot X-ray absorption spectroscopy

## Single shot EXAFS and XANES

### Next to the edge

- information about the ions
- Ionic structure, ion temperature

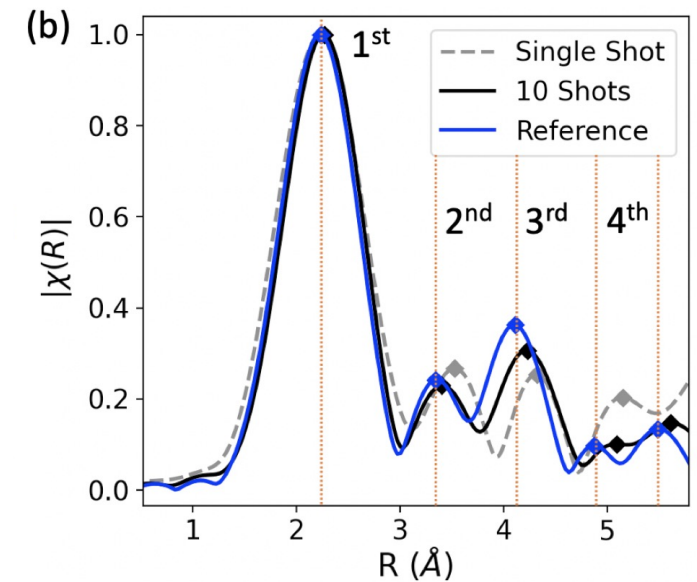
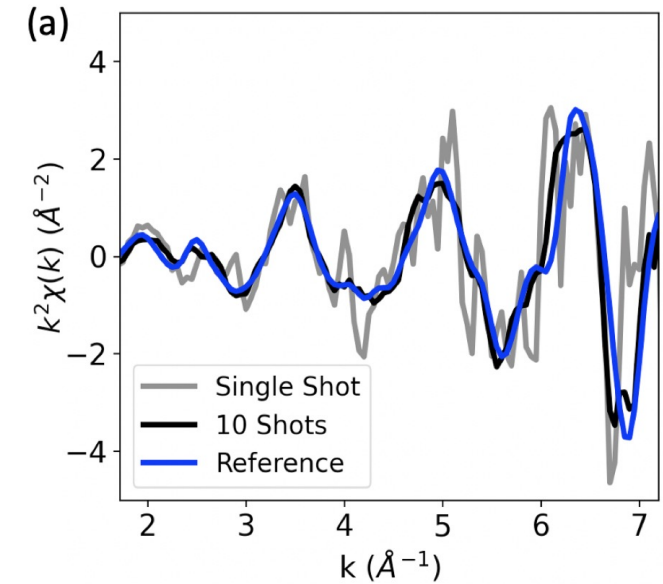


# Single shot X-ray absorption spectroscopy

## Single shot EXAFS and XANES

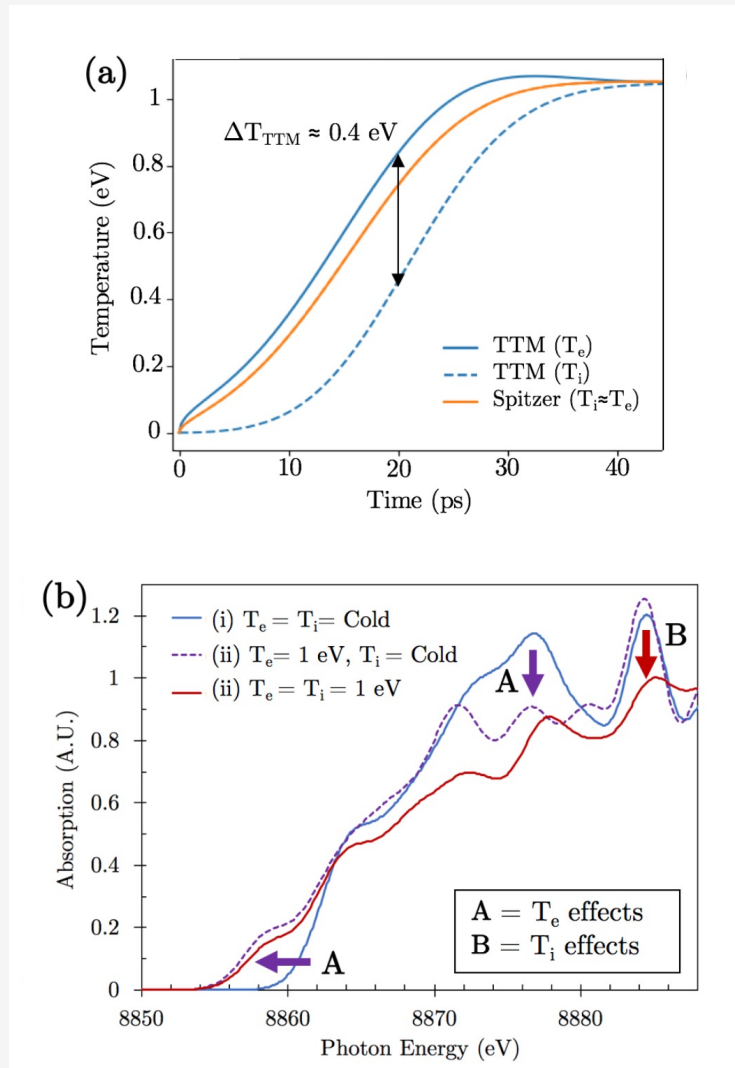
### Next to the edge

- information about the ions
- Ionic structure, ion temperature
- Here we show measurement of position of first four nearest neighbours (coordination shells)
  - Single shot accuracy of 1.5% (shells 1) and 5% (shells 2 – 4)



# What's next?

## Pump Probe Experiments

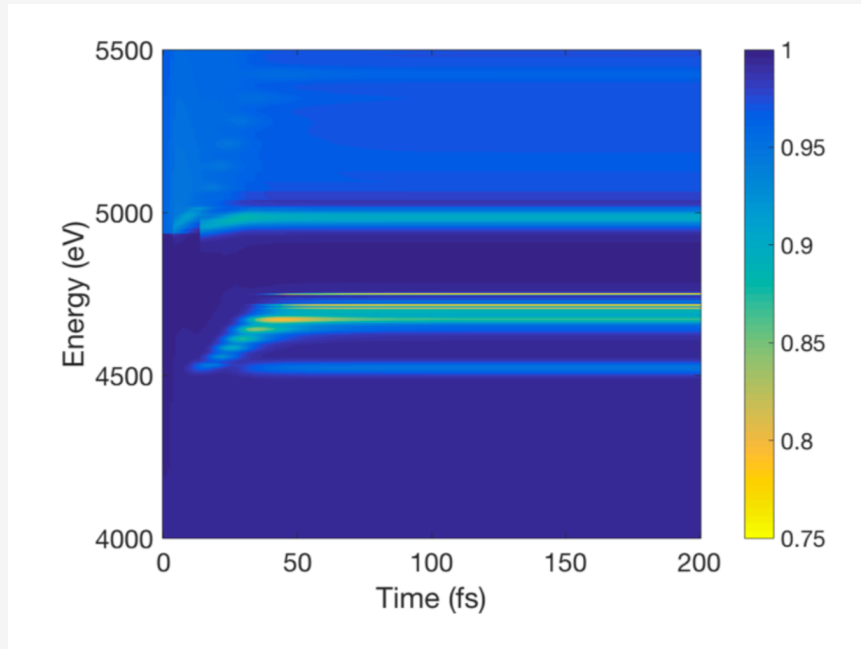


### Pump-probe experiment to measure rate of heat flow between ions in warm dense matter

- warm dense matter created by picosecond x-ray heating (picosecond laser drive)
- investigate coupling between ions and electrons
  - Ion density fluctuations – phonons
  - Ion charge fluctuations (see Baggott PRL 2021)

# What's next?

## Pump Probe Experiments



### Pump-probe experiment to measure rate of ionization in hot dense plasma

- Hot dense plasma created by fast electron heating (femtosecond laser drive)
  - Measure change in opacity on route to equilibrium: testing NLTE codes
  - Time-resolved measurements of plasma opacity in conditions relevant to solar interior

# IMPERIAL

## Summary:

### 1 Intro to laser wakefield accelerators

GeV electron beams  
femtosecond beam

### 2 Basic concepts of X-ray generation

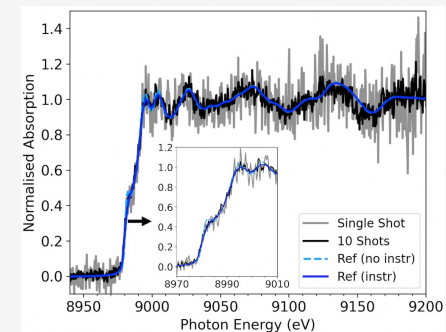
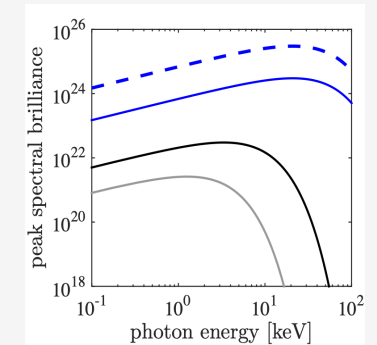
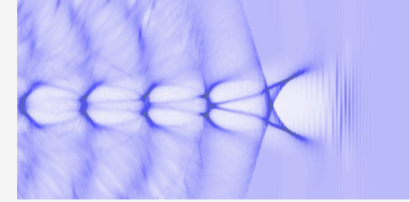
synchrotron radiation  
wigglers, undulators and FELs

### 3 Synchrotron radiation from Laser Wakefield Accelerators

betatron oscillations  
femtosecond, broadband x-rays

### 4 Applications of X-rays from Laser Wakefield Accelerators

ultrafast imaging  
ultrafast XAS



# IMPERIAL

# Thank you

LWFA: Tools for Time-Resolved X-Ray Imaging and Spectroscopy  
23/04/2024

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